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B.E. (Illrd Sem.) (CGPA) (CSE) Examination-2015

MATHEMATICS-II

Paper : CS-301

Time Allowed : Three Hours

Maximum Marks : 60

Note : Attempt all questions.

Each question carry equal marks.

Q.I Solve any two of the following—

(a) Solve $\frac{dy}{dx} + 2y \tan x = \sin x$, given that $y = 0$, when

$$x = \frac{\pi}{3}$$

(b) Solve —

$$(x^2 + y^2 + 2x) dx + 2y dy = 0$$

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P.T.O.

(2)

(c) Solve $x^2 p^3 + y(1+x^2 y) p^2 + y^3 p = 0$ where

$$p = \frac{dy}{dx}$$

(d) Solve $(x^2 - a^2) p^2 - 2xy p + y^2 - b^2 = 0$ where

$$p = \frac{dy}{dx}$$

Q.II Solve any two—

(a) Solve —

$$\frac{d^3 y}{dx^3} - 3 \frac{d^2 y}{dx^2} + 9 \frac{dy}{dx} - 27 y = \cos 3x$$

(b) Solve—

$$\frac{d^2 y}{dx^2} + 4y = x^2 + \cos^2 x$$

(c) Solve $x^2 \frac{d^2 y}{dx^2} + x \frac{dy}{dx} - y = 0$, given that $x + \frac{1}{x}$ is

one integral.

(d) Solve $\frac{d^2 y}{dx^2} - 2 \tan x \frac{dy}{dx} + 5y = \sec x \cdot e^x$

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Contd.

(3)

Q.III Solve any two —

(a) Change the order of integration of the

$$\int_0^3 \int_1^{\sqrt{4-y}} (x+y) dx dy$$

(b) Evaluate $\iint_R xy dx dy$, over the region in R the

positive quadrant for which $x+y \leq 1$.

(c) Prove that $\int_0^1 x^5 (1-x^3)^{10} dx = \frac{1}{262}$.

(d) Evaluate $\int_0^1 \left\{ \log \frac{1}{y} \right\}^{n-1} dy$

Q.IV Solve any two of the following—

(a) Prove that $L \left\{ \sin \sqrt{t} \right\} = \frac{\sqrt{\pi} e^{-1/4s}}{2s^{3/2}}$

(b) Find the Laplace transform of $\int_0^t \frac{\sin t}{t} dt$

(4)

(c) Find $L^{-1} \left\{ \frac{5s+3}{(s-1)(s^2+5s+6)} \right\}$

(d) Solve the differential equation by Laplace

transformation method $\frac{d^2y}{dt^2} - 3\frac{dy}{dt} + 2y = 4t + e^{3t}$,

when $y(0)=1$ and $y'(0)=-1$.

Q.V Solve any two of the following—

(a) Find the Fourier series to represent $x-x^2$ from $-\pi$ to π .

(b) Find the Fourier series to represent the function, if—

$$f(x) = \begin{cases} -\pi, & -\pi < x < 0 \\ x, & 0 < x < \pi \end{cases}$$

(c) Express $f(x)=x$ as a half range sine series in $0 < x < 2$.

(d) Find the Fourier series as far as the second harmonic to represent the function given by the following table—

x:	0	1	2	3	4	5
y = f(x):	4	8	15	7	6	2